

Vertical Fibers

Horizontal fibers

Bulk : $P(t)$

Membrane

Equilibrium at the contact:

$$P \pi R^2 \tan^2(\varphi) + \sigma_{fv} A_f = F$$

Equilibrium at the apex:

$$T + h_0 \sigma_{fh} = PR/2$$

Inject the expressions relating the stresses to $R(t)$ and $\varphi(t)$ in these equations

Then I have 2 non linear equations of 2 unknowns

Numerical resolution



4 components:

Vertical Fibers

Horizontal fibers

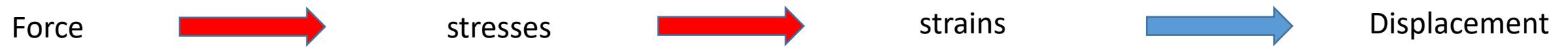
Bulk

Membrane

membrane

$$W = \int T dE$$

$$T = \partial W / \partial E = Y (E+E')$$



4 components:

Vertical Fibers

Horizontal fibers

Bulk

Membrane

fibers

$$W = \int \sigma_f dE$$

$$\sigma_f = \partial W / \partial E$$



4 components:

Vertical Fibers

Horizontal fibers

Bulk

Membrane

bulk

$$W = \int P \, dJ$$

$$P = \partial W / \partial J = K(J-1)$$



Vertical Fibers

Horizontal fibers

Bulk

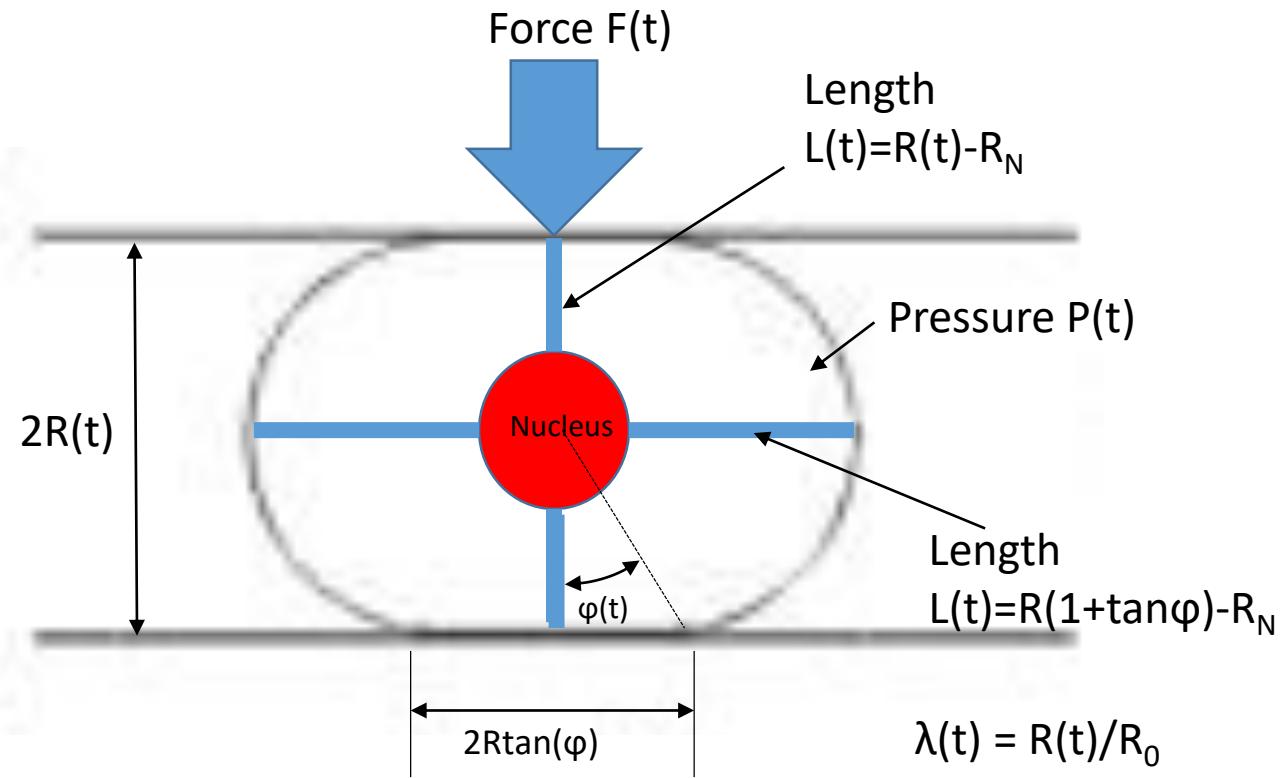
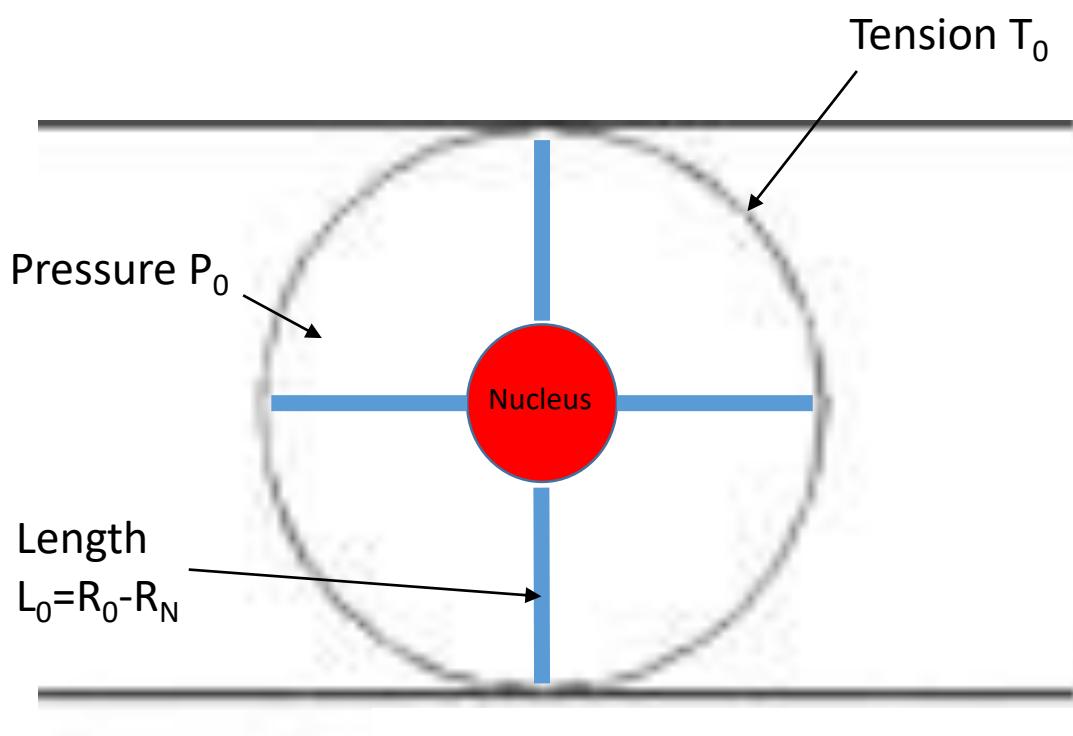
Membrane

$$J = V/V_0 = (R/R_0)^3 [3/2 \tan^2(\varphi) + 3\pi/4 \tan(\varphi) + 1]$$

$$E = (R/R_0)^2 [\tan(\varphi) + \tan^2(\varphi)/2]$$

$$E_{fv} = [((R - R_N)/(R_0 - R_N))^2 - 1] / 2$$

$$E_{fh} = [[(R(1+\tan\varphi) - R_N)/(R_0 - R_N)]^2 - 1] / 2$$



Energy per unit area

For the membrane

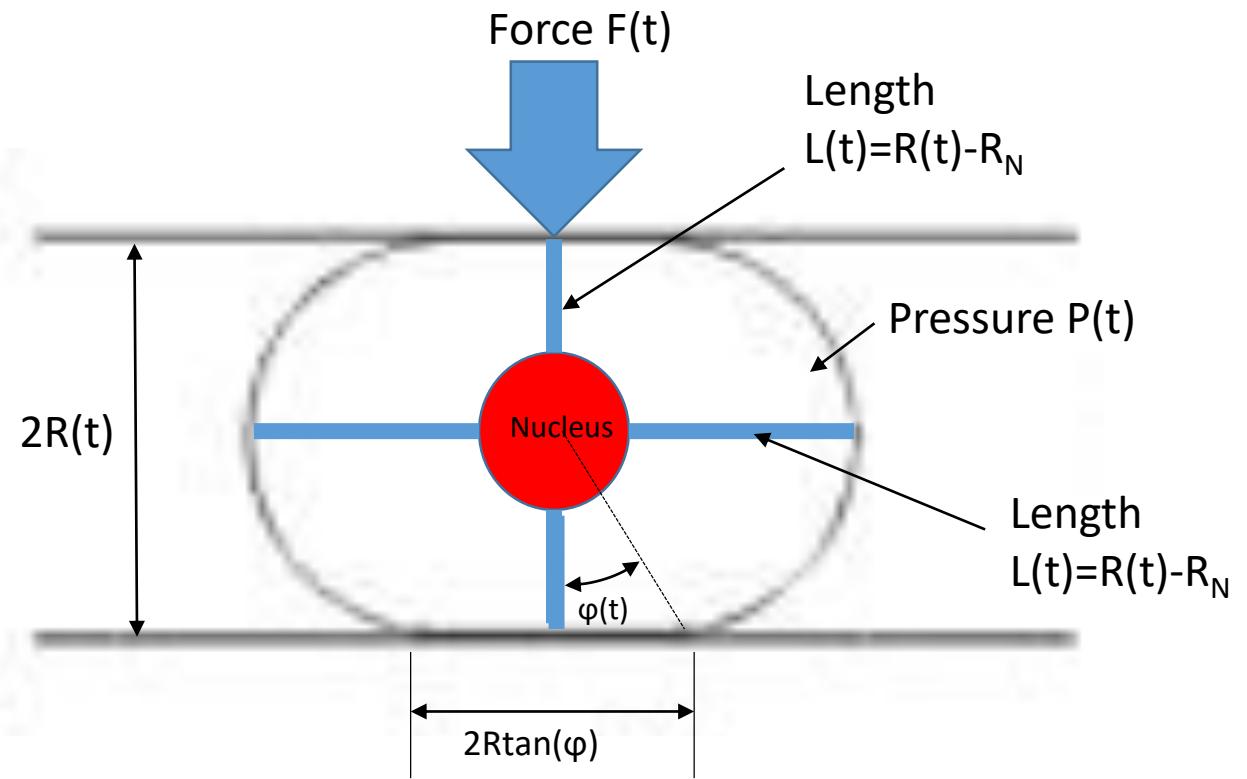
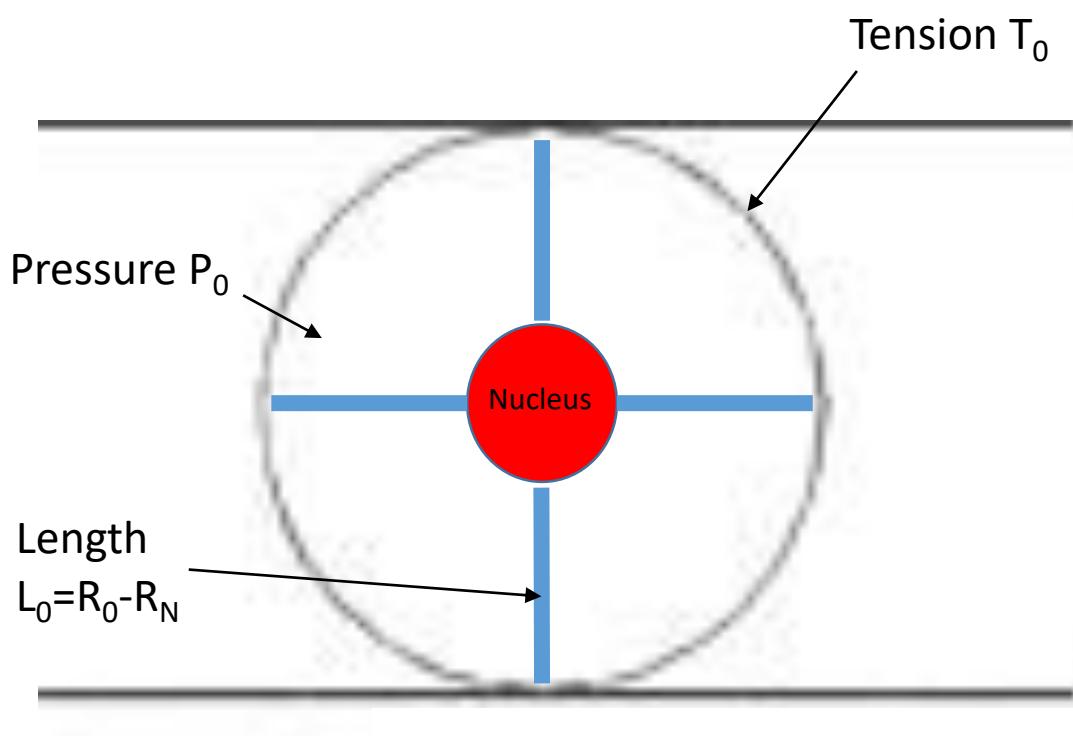
$$W(E) = Y/2 (E + E')^2$$

E' is the prestrain

$$E = S/S_0 - 1$$

$$S = 4 \pi R^2 [1 + \tan(\varphi) + \tan^2(\varphi)/2]$$

$$S_0 = 4 \pi R_0^2$$

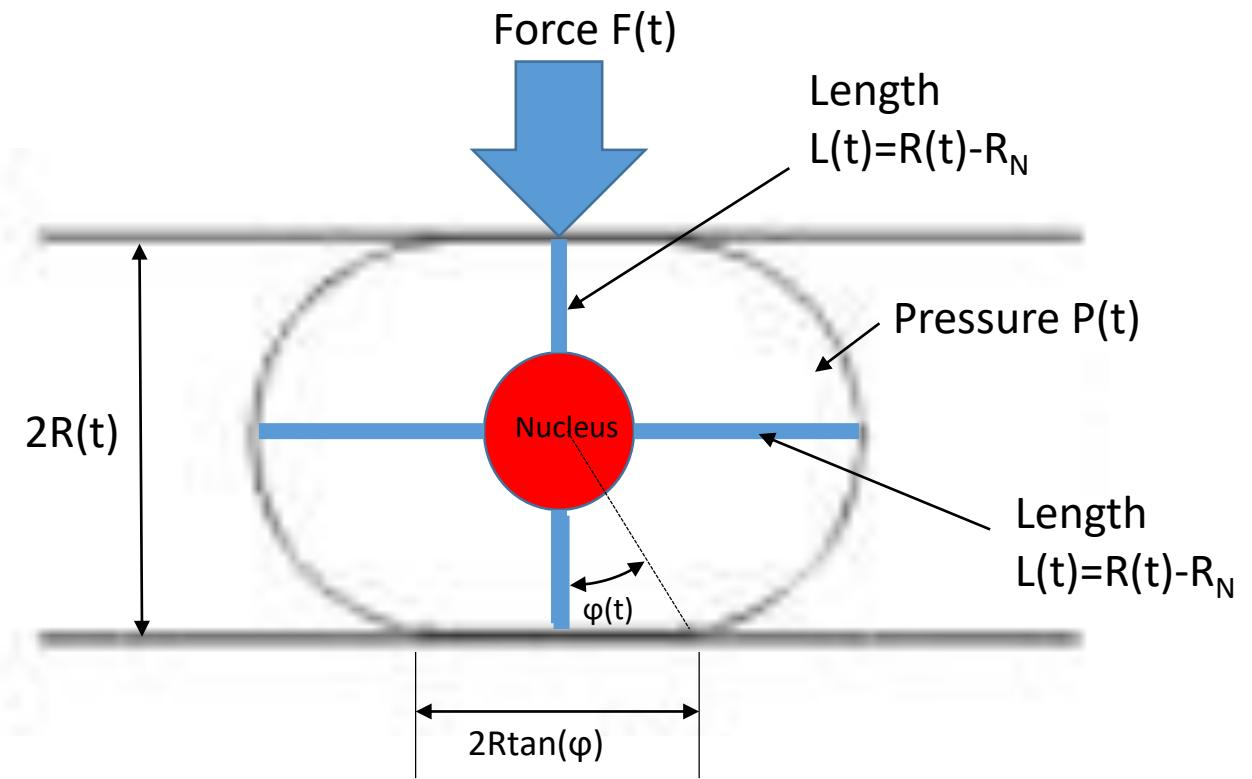
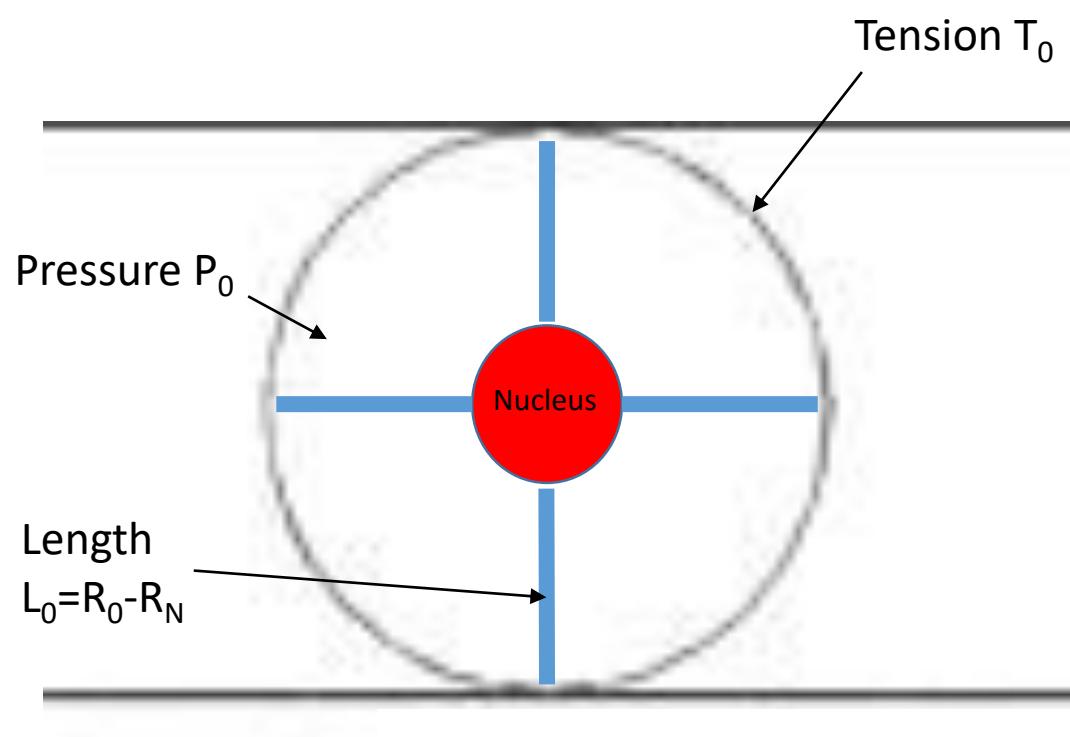


For the bulk

$$W(J) = K/2 (J-1)^2$$

$$J = V/V_0$$

$$\begin{aligned} V &= V_0 \\ V &= 2\pi R^3 \tan^2(\varphi) + \pi^2 R^3 \tan(\varphi) + 4/3 \pi R^3 \\ V &= 4/3 \pi R^3 [3/2 \tan^2(\varphi) + 3\pi/4 \tan(\varphi) + 1] \\ V_0 &= 4/3 \pi R_0^3 \end{aligned}$$



For the fibers

$$W(E) = k/2 E^2 \text{ if } E < 0$$

$$W(E) = k/2a [\exp(aE^2) - 1] \text{ if } E < 0$$

$$E = [(L/L_0)^2 - 1] / 2$$